Total No. of Questions : 9]

**PA-1182** 

SEAT No. :

[Total No. of Pages : 7

*P.T.O.* 

#### [5925]-204 S.E. (Civil) ENGINEERING MATHEMATICS - III (2019 Pattern) (Semester - III) (207001)

Time : 2<sup>1</sup>/<sub>2</sub> Hours | [Max. Marks: 70 Instructions to the candidates: 1) Question No. 1 is compulsory. 2) Attempt Q.2 or Q.3, Q.4 or Q.5, Q.6 or Q.7, Q.8 or Q.9. 3) Assume suitable data, if necessary. 4) Neat diagrams must be drawn wherever necessary. Figures to the right indicates full marks. 5) **6)** Use of electronic pocket calculator is allowed. The pair of regression Linens are L1 : 8x - 10y + 66 = 0 and *Q1*) a) L2:40x-18y=214[1] L1 is the regression Line y on xi) ii) L1 is the regression line x on y. L2 is regression line y or x. iii) L1 and L2 is regression line x on y. iv) Vector along the direction of the line. **b**) [1]  $\frac{x-1}{2} = \frac{y+2}{1} = \frac{z-3}{5}$  is ii)  $\frac{\hat{i}+2\hat{j}+5\hat{k}}{\sqrt{30}}$ i)  $\frac{\hat{i}-2\hat{j}-3\hat{k}}{\sqrt{14}}$ iii)  $\frac{2\hat{i}+\hat{j}-5\hat{k}}{\sqrt{20}}$ iv)  $\frac{2\hat{i}+\hat{j}+5\hat{k}}{\sqrt{20}}$ 

c) Let X = B(7,1/3) be the Binomial distribution with parameters n = 7 and p = 1/3. Then p(x = 2) + p(x = 5) is [2] i) 81/28 ii) 28/81

iii) 7/81 iv) 10/81

d) If vector field  $\mathbf{F} = (x+3y)\hat{j} + (y-2z)\hat{j} + (x+mz)\hat{k}$  is solenoidal the value of *m* is [2]

- i) –2 ii) 3
- iii) 2 iv) 0
- e) Using Stoke's theorem  $\iint_{c} \mathbf{F} \cdot d\mathbf{r}$  where  $\mathbf{F} = xy\hat{i} + y\hat{z}\hat{j} + z\hat{k}$  over the cube whose side is a and it's face in XOY plane is missing is equal to [2]
  - i) 0 ii)  $\iint_{\mathbb{R}} y \, dx \, dy$
  - iii)  $\iint_{R} 2x \, dx dy \, dx dy \, dx dy \, dx dy$

f) Most general solution of  $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$  is [2]

- i)  $u(x,t) = (c_1 \cos mx + c_2 \sin mx) (c_3 \cos cmt + c_4 \sin cm)$
- ii)  $u(x, t) = (c_4 \cos mx + c_5 \sin mx)e^{-m^2 t}$
- iii)  $u(x, t) = (c_1 e^{-mx} + c_2 e^{mx})(c_1 \cos my + c_2 \sin my)$

iv) 
$$u(x t) = (c_1 \cos mx + c_2 \sin mx)(c_3 e^{-my} + c_4 e^{my})$$

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#### 2

Q2) a) A computer while calculating carrelation coefficient between two variablesX and Y from 25 pairs of observations obtained the following results :

n = 25,  $\sum X \pm 25$ ,  $\sum X^2 = 650$ ,  $\sum Y \pm 00$ ,  $\sum Y^2 = 460$ ,  $\sum XY = 508$ .

Later it was discovered that the values (X, Y) = (8, 12) was copied as (6, 14) and the value (8, 6) was copied as (6, 8). Obtain the correct value of the correlation coefficient. [5]

- b) In a normal distribution 31% of the items are under 45 and 8% are above 64. Find the mean and standard deviation of the distribution. Take Area (0 < z < 1.4) = 0.42 and Area (0 < z < 0.5) = 0.19 where z is the standard normal variate. [5]
- c) Verify at 5% level of significance and 4 degrees of freedom if the distribution can be assumed to be poisson given:

# defects :	0	1	2	3	4	5
Frequency :	6	13	13	8	4	3

Take  $e^{-2} = 0.135$ . in the calculations round off the frequencies to the immediate higher integral value. Take $\chi^2_{0.05} = 11.07$  [5]

OR

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- **Q5)** a) Find the directional derivative of  $\phi = xy + yz^2$  at the point (1, -1, 1) to wards point (2, 1, 2). [5]
  - b) Prove the following identities (any one) [5] i)  $\nabla \times (\vec{a} \times \vec{r}) = 2\vec{a}$ 
    - ii)  $\nabla(\vec{a.r}) = \vec{a}$
  - c) Show that  $\vec{F} = (xy^2 + xz^2)\hat{i} + (yx^2 + yz^2)\hat{j} + (zx^2 + zy^2)\hat{k}$  is irrotational. Find scalar  $\phi$  such that  $\vec{F} = \nabla \phi$  [5]
- **Q6)** a) Evaluate  $\int_{c} \overline{F} \cdot d\overline{r}$  along the straight line joining points (0, 0, 0) and (2, 1, 3)where  $=\overline{F} = 3\sqrt{3}T + (2xz - y)\overline{j} + z\overline{k}$  [5]

b) Evaluate  $\iint_{s} (x\overline{i} + y\overline{j} + z\overline{k}) \cdot d\overline{s}$  over the surface of sphere  $x^{2} + y^{2} + z^{2} = 1$  [5]

c) Evaluate using Stoke's theorem  $\iint_{S} (\nabla \times \overline{F}) \cdot d\overline{s}$  where  $\overline{F} = y^{2}\overline{i} + z\overline{j} + xy\overline{k}$  and S is surface of paraboloid  $z = 4 - x^{2} - y^{2}(z \ge 0)$ . [5]

#### OR

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- **Q7)** a) Use Green's theorem to evaluate  $\int_{c} (2x^2 y^2) dx + (x^2 + y^2) dy$  where 'C' is boundary of area enclosed by the axis and circle  $x^2 + y^2 = 16, z = 0.$  [5]
  - b) Apply Stoke's theorem to evaluate  $\int_{c} \overline{F} \cdot d\overline{r}$  where  $\overline{F} = yz\overline{i} + zx\overline{j} + xy\overline{k}$  and S is upper part of sphere  $x^{2} + y^{2} + z^{2} = 1$  above XOY plane. [5]
  - c) Evaluate  $\iint_{s} (x\overline{i} + y\overline{j} + z^{2}\overline{k}) \cdot d\overline{s}$ . Where S is the surface of cylind  $e^{2} + y^{2} = 4$ bounded by planes z = 0 and z = 2. [5]
- **Q8)** a) A string stretched and fastened between two points L a part. Motion is started by displacing the string in the form  $y = a \sin \frac{\pi x}{L}$  from which it is released at time t = 0. Find the displacement (x, t). [8]
  - b) Solve the one almensional heat equation  $\frac{\partial y}{\partial t} = k \frac{\partial^2 u}{\partial x^2}$  subject to conditions.
    - i) u is finite  $\forall t$ .
    - ii) u(0,t) = 0,
    - iii)  $u(\pi, t) = 0$ ,
    - iv)  $u(x, 0) = \pi x x^2 \quad 0 \le x \le \pi$  [7]

OR

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- **Q9)** a) A tightly stretched string with fixed ends x = 0 and x = 1 is initially at rest in its equilibrium position is set to vibration by giving each point a velocity 3x(l-x) for 0 < x < l. Find the displacement y(x, t) at any time t. [8]
  - b) An infinitely long uniform metal plate is enclosed between lines y = 0, and y = l for x > 0. The temperature is zero along the edges y = 0, y = l, and at infinity. If edge x = 0 is kept at a constant temperature, Find the temperature distribution v(x,y).

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